



IRT or Rasch – what can and cannot be done?

WORKSHOP

L R Pendrill¹, and the EMPIR NeuroMet 15HLT04 consortium

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EXAM12

35 arthritis patients have been through rehabilitation therapy. Their admission to therapy and discharge from therapy measures are to be compared. They have been rated on the 13 mobility items of the Functional Independence Measure (FIM™).

Each item has seven levels.

At admission, the patients could not perform at the higher levels. At discharge, all patients had surpassed the lower levels (Data courtesy of C.V. Granger & B. Hamilton, ADS).

1	0% Independent
2	25% Independent
3	50% Independent
4	75% Independent
5	Supervision
6	Device
7	Independent



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A User's Guide to

WINSTEPS[®] MINISTEP

Rasch-Model
Computer Programs

Program Manual 3.81.0 by

John M. Linacre





```
; This common control file is EXAM12.TXT
TITLE='GENERIC ARTHRITIS FIM CONTROL FILE'
ITEM1=9 ; Responses start in column 9
NI=13 ; 13 mobility items
CODES=1234567 ; 7 level rating scale
CLFILE="" ; Defines the rating scale
1 0% Independent
2 25% Independent
3 50% Independent
4 75% Independent
5 Supervision
6 Device
7 Independent
*
@TIMEPOINT = $S7W1 ; the time-point code A=Admission, D=Discharge
PSUBTOTAL = @TIMEPOINT ; subtotals by time-point
&END
A. EATING
B. GROOMING
C. BATHING
D. UPPER BODY DRESSING
E. LOWER BODY DRESSING
F. TOILETING
G. BLADDER
H. BOWEL
I. BED TRANSFER
J. TOILET TRANSFER
K. TUB, SHOWER
L. WALK/WHEELCHAIR
M. STAIRS
END NAMES
```



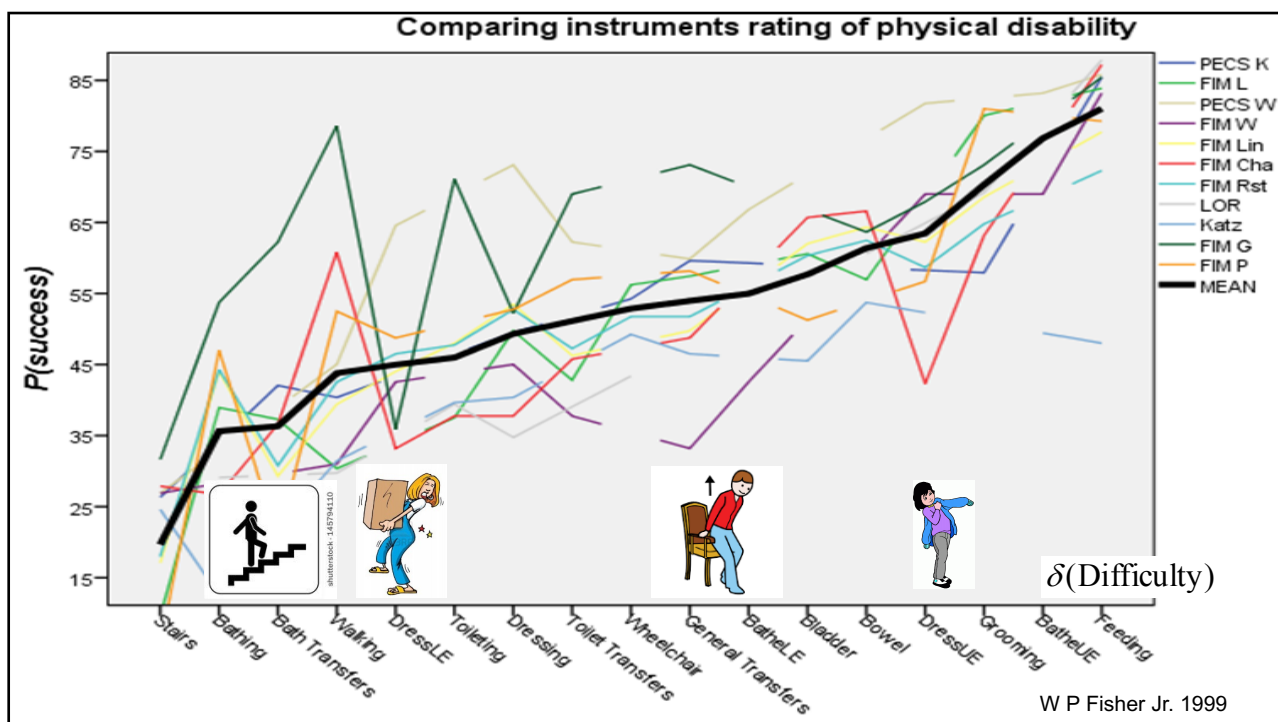
A User's Guide to **WINSTEPS®** **MINISTEP** Rasch-Model Computer Programs

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11.13 Example 12: Comparing high and low samples with rating scales



	A	B	C	D	E	F	G	H	I	J	K	L	M	N
1	TP	A. EATING	B. GROOMING	C. BATHING	D. UPPER BODY DRESSING	E. LOWER BODY DRESSING	F. TOILETING	G. BLADDER	H. BOWEL	I. BED TRANSFER	J. TOILET TRANSFER	K. TUB, SHOWER	L. WALK/WHEELCHAIR	M. STAIRS
2	21101	5	5	2	3	1	3	3	3	2	2	1	2	1
3	21170	4	4	3	3	4	4	3	3	4	5	4	5	4
4	21174	4	4	4	4	3	4	4	4	3	4	1	4	1
5	21191	4	4	4	4	2	4	4	4	4	4	3	4	4
6	21243	4	2	2	1	1	2	2	2	1	1	1	1	1
7	21250	3	2	1	2	2	2	4	4	4	4	4	5	1
8	21266	4	4	3	4	2	3	5			4	3		



Score, x

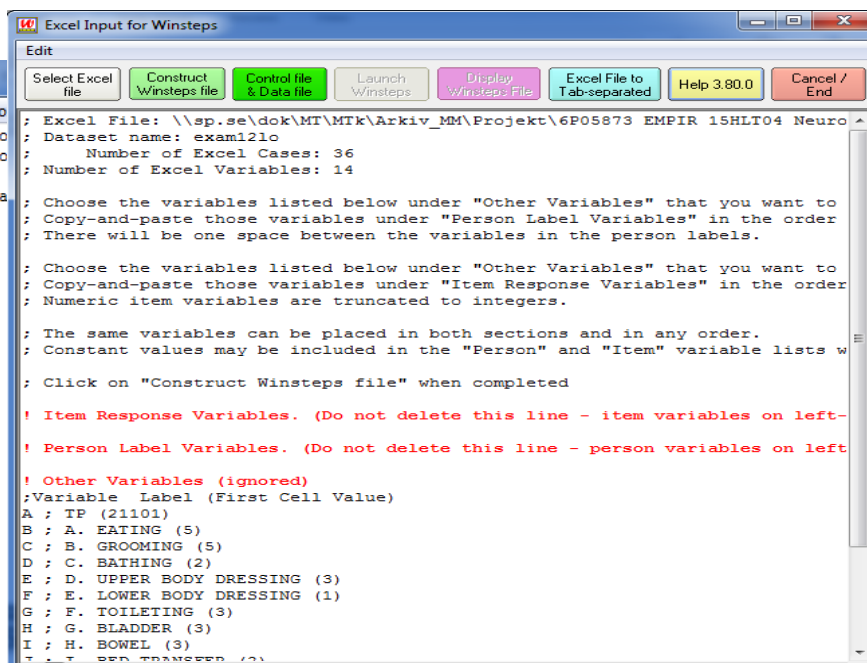
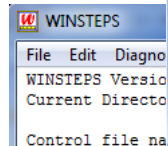
- 1 0% Independent
- 2 25% Independent
- 3 50% Independent
- 4 75% Independent
- 5 Supervision
- 6 Device
- 7 Independent



Illustration: 1.59794110

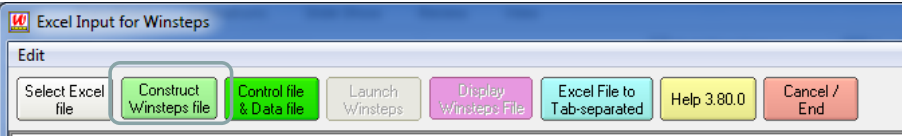


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Excel Input for Winsteps

Edit

Select Excel file Construct Winsteps file Control file & Data file Launch Winsteps Display Winsteps File Excel File to Tab-separated Help 3.80.0 Cancel / End

! Item Response Variables. (Do not delete this line - item variables on left-side if this line before "Person Label Variables")

B ; A. EATING (5)
C ; B. GROOMING (5)
D ; C. BATHING (2)
E ; D. UPPER BODY DRESSING (3)
F ; E. LOWER BODY DRESSING (1)
G ; F. TOILETING (3)
H ; G. BLADDER (3)
I ; H. BOWEL (3)
J ; I. BED TRANSFER (2)
K ; J. TOILET TRANSFER (2)
L ; K. TUB, SHOWER (1)
M ; L. WALK/WHEELCHAIR (2)
N ; M. STAIRS (1)

! Person Label Variables. (Do not delete this line - person variables on left-side if before "Item Response Variables")

A ; TP (21101)

! Other Variables (ignored)

;Variable Label (First Cell Value)

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Excel Input for Winsteps

Edit

Select Excel file Construct Winsteps file Control file & Data file Launch Winsteps Display Winsteps File Excel File to Tab-separated Help 3.80.0 Cancel / End

Exam12loe_new_190421 - Anteckningar

Arkiv Redigera Format Visa Hjälp

```
&INST
Title= "\\sp.se\dok\MT\MTK\Arkiv_MM\Projekt\6P05873 EMPIR 15HLT04 NeuroMet_2016\Ppresentations\2019\PM_Health_2019\workshop
\exam12\Exam12loe_new_190421.xls"
; Excel File created or last modified: 2019-04-22 07:21:05
; exam12loe
;
; Excel Cases processed = 36
; Excel Variables processed = 14
ITEM1 = 1 ; Starting column of item responses
NI = 13 ; Number of items
NAME1 = 15 ; Starting column for person label in data record
NAMELEN = 6 ; Length of person label
XWIDE = 1 ; Matches the widest data value observed
; GROUPS = 0 ; Partial Credit model: in case items have different rating scales
CODES = "12345 " ; matches the data
TOTALSCORE = Yes ; Include extreme responses in reported scores
; Person Label variables: columns in label: columns in line
&TP = 1E5 ; $C15W5
&END ; Item labels follow: columns in label
A. EATING ; Item 1 : 1-1
B. GROOMING ; Item 2 : 2-2
C. BATHING ; Item 3 : 3-3
D. UPPER BODY DRESSING ; Item 4 : 4-4
E. LOWER BODY DRESSING ; Item 5 : 5-5
F. TOILETING ; Item 6 : 6-6
G. BLADDER ; Item 7 : 7-7
H. BOWEL ; Item 8 : 8-8
I. BED TRANSFER ; Item 9 : 9-9
J. TOILET TRANSFER ; Item 10 : 10-10
K. TUB, SHOWER ; Item 11 : 11-11
L. WALK/WHEELCHAIR ; Item 12 : 12-12
M. STAIRS ; Item 13 : 13-13
END NAMES
5523133322121 21101
4433443345454 21170
4444344434141 21174
4444344434141 21174
```

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Excel Input for Winsteps

Edit

Select Excel file Construct Winsteps file Control file & Data file Launch Winsteps Display Winsteps File Excel File to Tab-separated Help 3.80.0 Cancel / End

Exam12loe_new_190421.txt

File Edit Diagnosis Output Tables Output Files Batch Help Specification Plots Excel/RSSST Graphs Data Setup

WINSTEPS Version 3.91.2 Apr 22 2019 7:35
Current Directory: \\sp.se\dok\MT\MTk\Arkiv_MM\Projekt\6P05873 EMPIR 15HLT04 NeuroMet_2016\Presentations\2019\PM_Health_2019\workshop\exam12\

Name of control file:
\\sp.se\dok\MT\MTk\Arkiv_MM\Projekt\6P05873 EMPIR 15HLT04 NeuroMet_2016\Presentations\2019\PM_Health_2019\workshop\exam12\Exam12loe_new_190421.t

Report output file name (or press Enter for temporary file, Ctrl+O for Dialog Box):

Extra specifications (if any). Press Enter to analyze:
Boxnumber=no

Calculating Fit Statistics
Time for estimation: 0:0:0.205
Processing Table 0
\\sp.se\dok\MT\MTk\Arkiv_MM\Projekt\6P05873 EMPIR 15HLT04 NeuroMet_2016\Presen

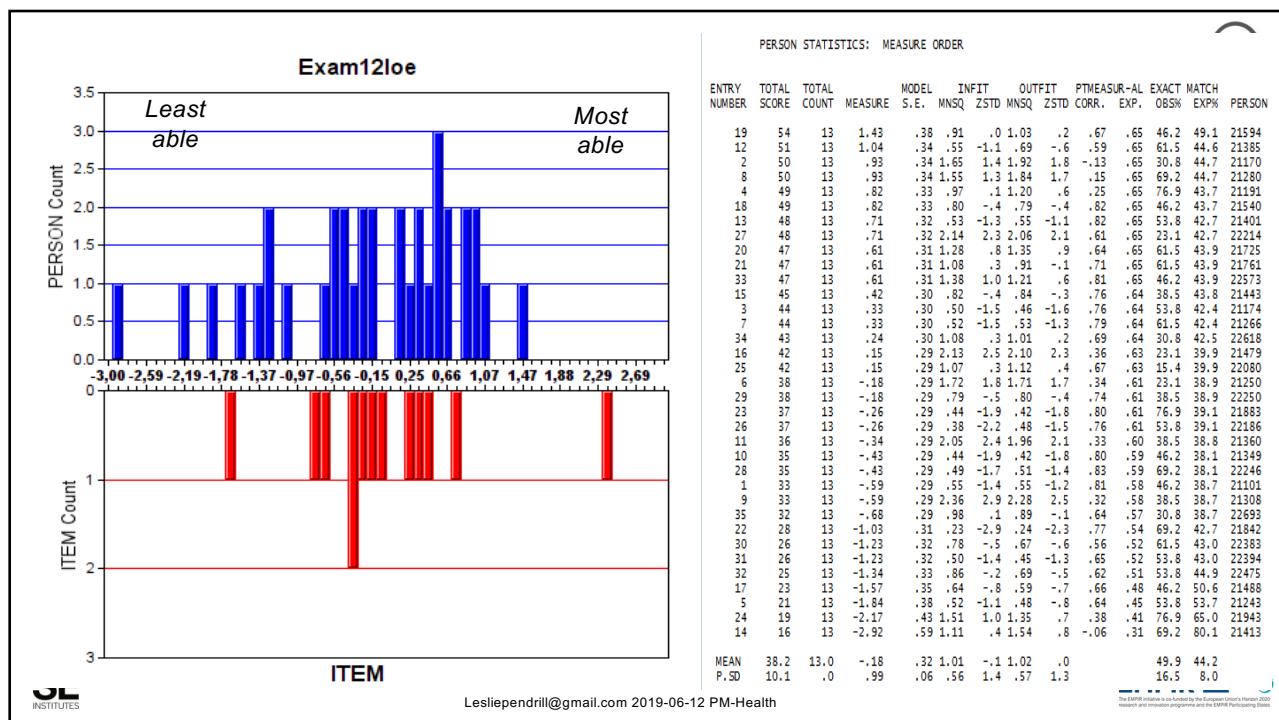
PERSON	35 INPUT	35 MEASURED	INFIT	OUTFIT			
TOTAL	COUNT	MEASURE	REALSE	IMNSQ	ZSTD	OMNSQ	ZSTD
MEAN	38.2	13.0	-.18	.35	1.01	-.1	1.02
P.SD	10.1	.0	.99	.08	.56	1.4	.57
REAL RMSE	.36	TRUE SD	.92	SEPARATION	2.54	PERSON RELIABILITY	.87

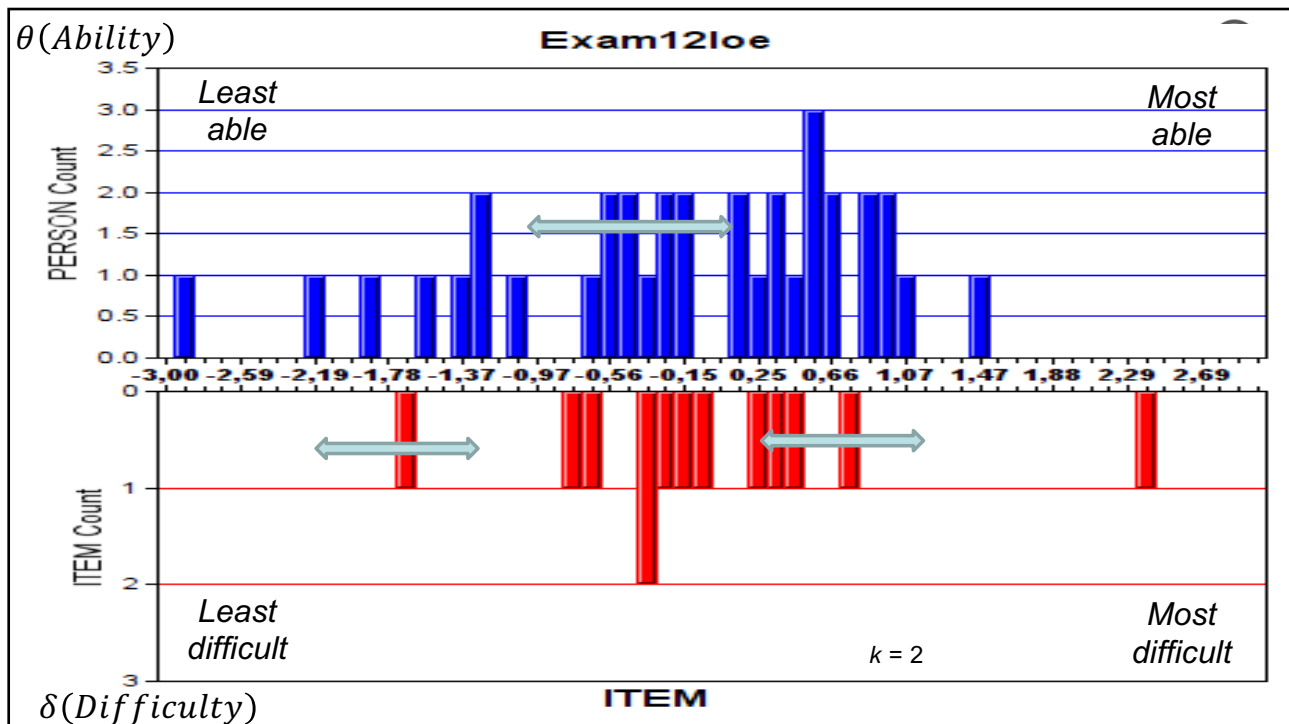
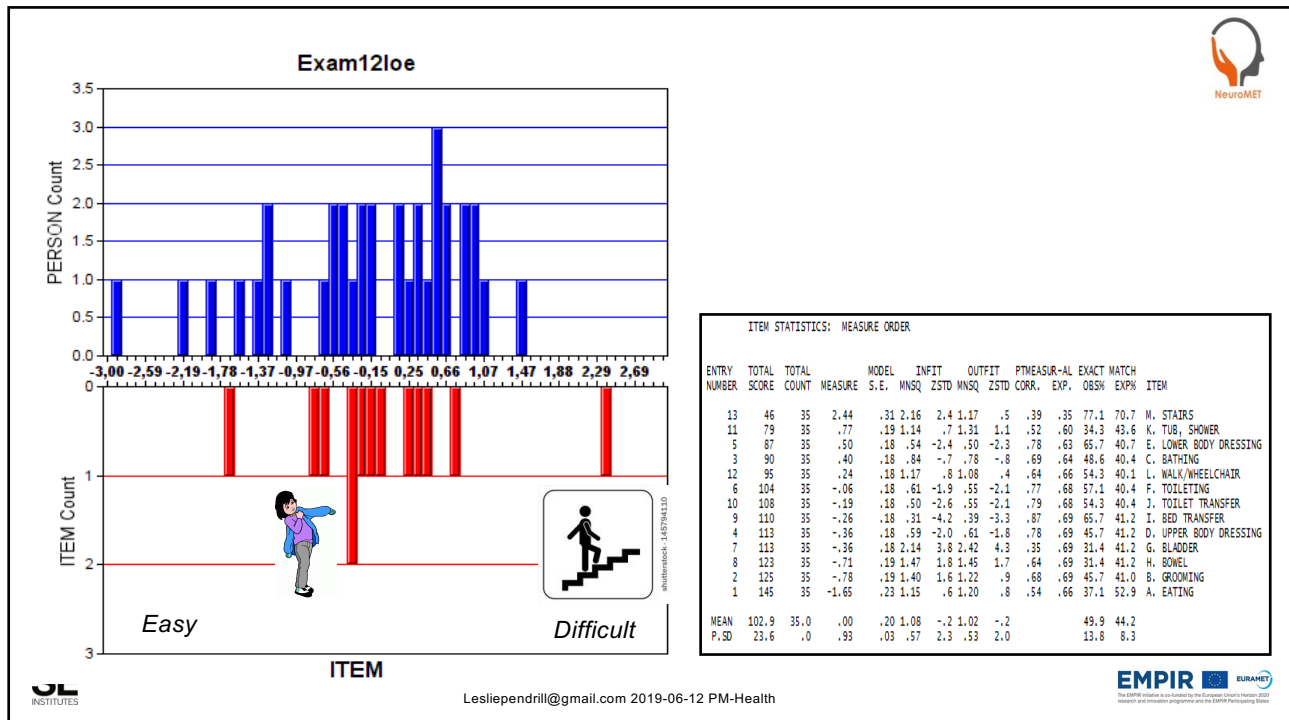
ITEM	13 INPUT	13 MEASURED	INFIT	OUTFIT			
TOTAL	COUNT	MEASURE	REALSE	IMNSQ	ZSTD	OMNSQ	ZSTD
MEAN	102.9	35.0	.00	.22	1.08	-.2	1.02
P.SD	23.6	.0	.93	.07	.57	2.3	.53
REAL RMSE	.24	TRUE SD	.90	SEPARATION	3.81	ITEM RELIABILITY	.94

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Exam12loe_new_190421.txt
File Edit Diagnosis Output Tables Output Files Batch Help Specification Plots Excel/RSSST Graphs Data Setup

13-042WS - Anteckningar

Arkiv Redigera Format Visa Hjälp

TABLE 13.1 \\sp.se\dok\MT\MTk\Arkiv_MM\Projekt\6 ZOU042WS.TXT1 Apr 22 2019 7:3516\Presenta
 INPUT: 35 PERSON 13 ITEM REPORTED: 35 PERSON 13 ITEM 5 CATS WINSTEPS 3.91.2

PERSON: REAL SEP.: 2.54 REL.: .87 ... ITEM: REAL SEP.: 3.81 REL.: .94

ITEM STATISTICS: MEASURE ORDER

ENTRY NUMBER	TOTAL SCORE	TOTAL COUNT	MEASURE	MODEL S.E.	INFI MNSQ	OUTFI ZSTD	PTMEASUR-AL CORR.	EXACT EXP.	MATCH OBS%	MATCH EXP%	ITEM		
13	46	35	2.44	.31	2.16	2.4	1.17	.5	.39	.35	77.1	70.7	M. STAIRS
11	79	35	.77	.19	1.14	.7	1.31	1.1	.52	.60	34.3	43.6	K. TUB, SHOWER
5	87	35	.50	.18	.54	-2.4	.50	-2.3	.78	.63	65.7	40.7	E. LOWER BODY DRESSING
3	90	35	.40	.18	.84	-.7	.78	-.8	.69	.64	48.6	40.4	C. BATHING
12	95	35	.24	.18	1.17	.8	1.08	.4	.64	.66	54.3	40.1	L. WALK/WHEELCHAIR
6	104	35	-.06	.18	.61	-1.9	.55	-2.1	.77	.68	57.1	40.4	F. TOILETING
10	108	35	-.19	.18	.50	-2.6	.55	-2.1	.79	.68	54.3	40.4	J. TOILET TRANSFER
9	110	35	-.26	.18	.31	-4.2	.39	-3.3	.87	.69	65.7	41.2	I. BED TRANSFER
4	113	35	-.36	.18	.59	-2.0	.61	-1.8	.78	.69	45.7	41.2	D. UPPER BODY DRESSING
7	113	35	-.36	.18	2.14	3.8	2.42	4.3	.35	.69	31.4	41.2	G. BLADDER
8	123	35	-.71	.19	1.47	1.8	1.45	1.7	.64	.69	31.4	41.2	H. BOWEL
2	125	35	-.78	.19	1.40	1.6	1.22	.9	.68	.69	45.7	41.0	B. GROOMING
1	145	35	-1.65	.23	1.15	.6	1.20	.8	.54	.66	37.1	52.9	A. EATING
MEAN	102.9	35.0	.00	.20	1.08	-.2	1.02	-.2			49.9	44.2	
P. SD	23.6	.0	.93	.03	.57	2.3	.53	2.0			13.8	8.3	



Illustration: 148794110



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34	22573	5	5	1
35	22618	4	4	3
36	22693	3	5	2
37	Mean	4.1	3.6	2.6
38	SD mea	0.2	0.2	0.2
39	TP	A. EATING	B. GROOMING	C. BATHING

Score, x

- 1 0% Independent
- 2 25% Independent
- 3 50% Independent
- 4 75% Independent
- 5 Supervision
- 6 Device
- 7 Independent



=AVERAGE(B2:B36)

CTT mean of
response x

$$\hat{x}_j = \frac{1}{N_{TP}} \cdot \sum_{i=1}^{N_{TP}} x_{i,j}$$

=STDEV(B2:B36)/SQRT(COUNTA(B2:B36))

u(CTT mean of
response x)

$$u(\hat{x}_j) = \frac{1}{N_{TP} \cdot (N_{TP} - 1)} \cdot \sum_{i=1}^{N_{TP}} (x_{i,j} - \hat{x}_j)^2$$

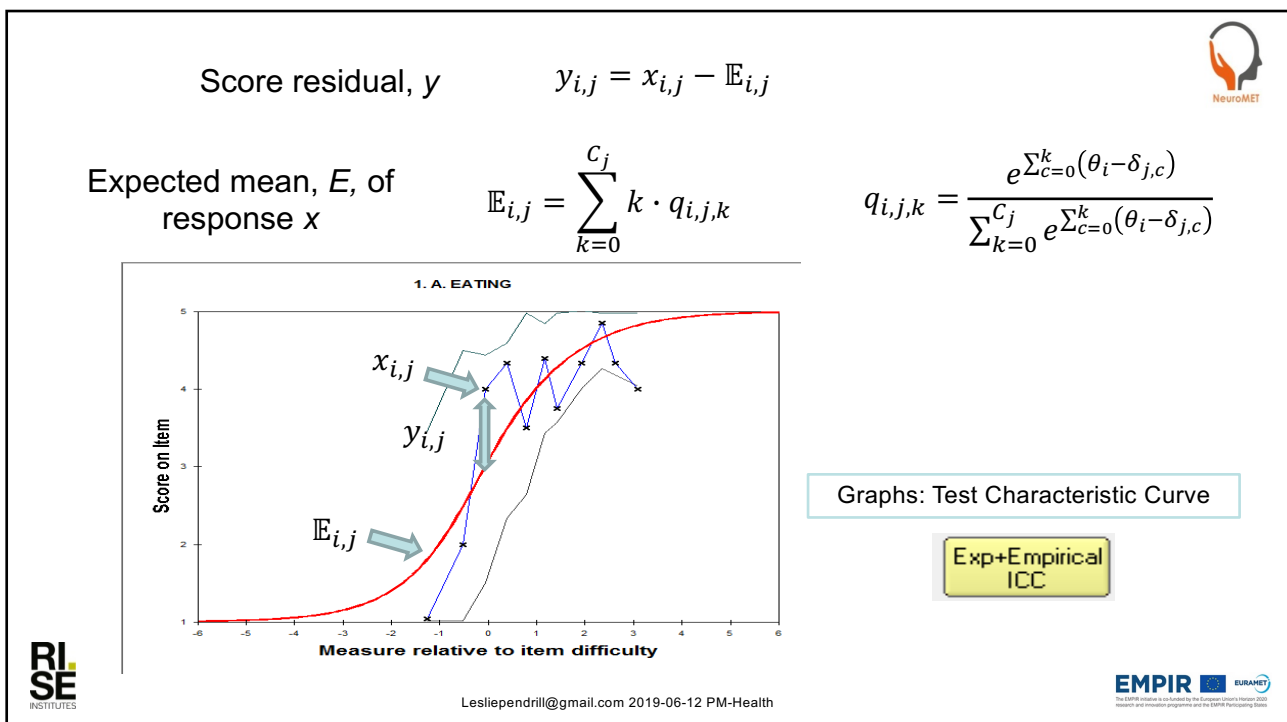
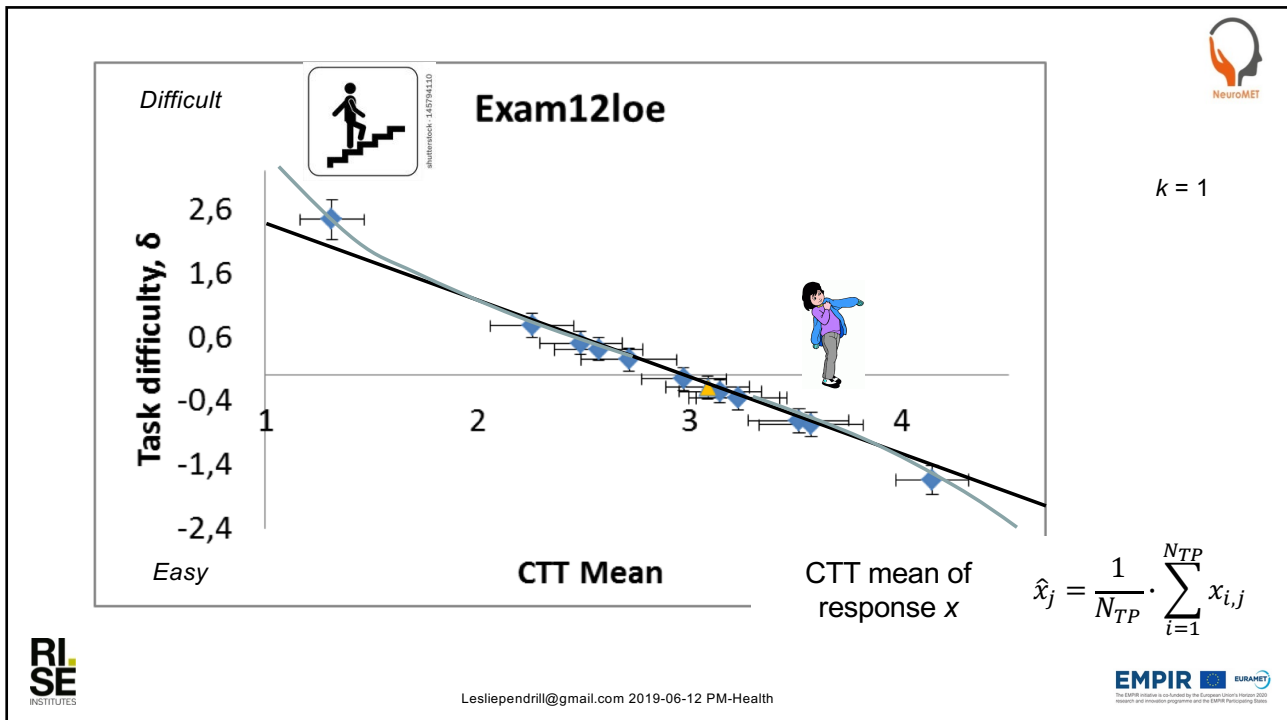
k = 1



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Score residual, y

$$y_{i,j} = x_{i,j} - \mathbb{E}_{i,j}$$

Expected mean, E , of response x

$$\mathbb{E}_{i,j} = \sum_{k=0}^{C_j} k \cdot q_{i,j,k}$$

$$q_{i,j,k} = \frac{e^{\sum_{c=0}^k (\theta_i - \delta_{j,c})}}{\sum_{k=0}^{C_j} e^{\sum_{c=0}^k (\theta_i - \delta_{j,c})}}$$

$$X = \chi_j^2 = \sum_{i=1}^{N_{TP}} y_i^2$$

$$INFIT_zstd_WH = \frac{2 \cdot \left(\sqrt[3]{X} - \sqrt[3]{N_{TP} - \frac{2}{3}} \right)}{\sigma}$$

$$\sigma = \frac{\sqrt{2}}{3 \cdot \sqrt[6]{N_{TP} - \frac{2}{3}}}$$

Molton: "Both statistics ... require a lot of meditation and incense.
For useful explanations, refer to:

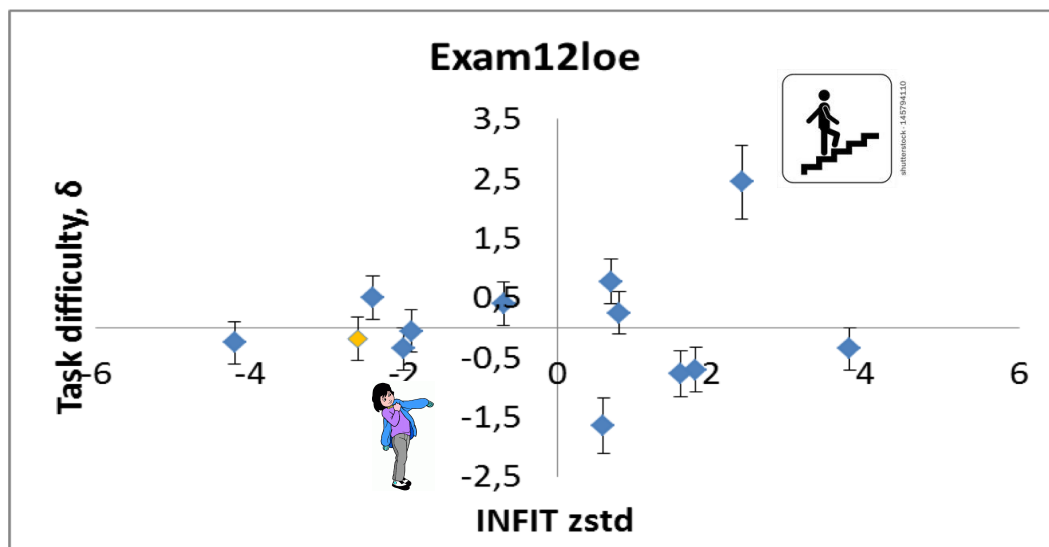
<http://www.rasch.org/rmt/rmt162f.htm>".



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Physical disability



$k = 2$



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EMPIR **EURAME**

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CON- TRAST	LOADING MEASURE	INFIT MNSQ	OUTFIT MNSQ	ENTRY NUMBER	ENTRY ITEM
1 1	.77	-.78	1.40	1.22	A 2 B. GROOMING
1 1	.72	-.36	.59	.61	B 4 D. UPPER BODY DRESSING
1 1	.63	-.40	.84	.78	C 3 C. BATHING
1 2	-.32	-.15	1.15	1.43	E 1 A. EATING
1 2	.28	-.50	.54	.50	E 5 E. LOWER BODY DRESSING
1 2	.25	-.06	.61	.55	F 6 F. TOILETING
1 3	-.74	-.24	1.17	1.08	A 12 L. WALK/ WHEELCHAIR
1 3	-.55	-.19	.50	.55	b 10 J. TOILET TRANSFER
1 3	-.39	-.26	.31	.39	c 9 I. BED TRANSFER
1 3	-.44	-.77	1.14	1.31	d 11 K. TUB, SHOWER
1 2	-.24	-.36	1.24	1.42	e 7 G. BLADDER
1 2	-.20	2.44	2.16	1.17	f 13 M. STAIRS
1 2	-.16	-.74	1.47	1.45	G 8 H. BOWEL

Calculating Fit Statistics
 >=====<
 Time for estimation: 0:0:0.205
 Processing Table 0
 \\sp.se\dok\MT\MTk\Arkiv_MM\Projekt\6P05873 EMPIR 15HLT04 NeuroMet_2016\Presen

Physical disability



PERSON	35 INPUT	35 MEASURED	INFIT		OUTFIT			
	TOTAL	COUNT	MEASURE	REALSE	IMNSQ	ZSTD	OMNSQ	ZSTD
MEAN	38.2	13.0	-.18	.35	1.01	-.1	1.02	.0
P.SD	10.1	.0	.99	.08	.56	1.4	.57	1.3
REAL RMSE	.36	TRUE SD	.92	SEPARATION	2.54	PERSON RELIABILITY	.87	

ITEM	13 INPUT	13 MEASURED	INFIT		OUTFIT			
	TOTAL	COUNT	MEASURE	REALSE	IMNSQ	ZSTD	OMNSQ	ZSTD
MEAN	102.9	35.0	.00	.22	1.08	-.2	1.02	-.2
P.SD	23.6	.0	.93	.07	.57	2.3	.53	2.0
REAL RMSE	.24	TRUE SD	.90	SEPARATION	3.81	ITEM RELIABILITY	.94	

$$J. TOILET TRANSFER_{ACQUI} = 7 - J. TOILET TRANSFER$$

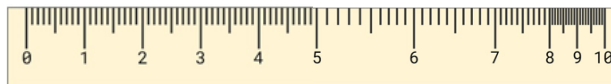
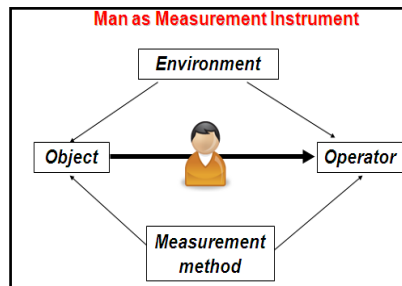
K
J. TOILET TRANSFER_ACQUI
5
2
3
3

PERSON	35 INPUT	35 MEASURED	INFIT		OUTFIT			
	TOTAL	COUNT	MEASURE	REALSE	IMNSQ	ZSTD	OMNSQ	ZSTD
MEAN	39.1	13.0	-.87	.31	1.02	-.1	1.01	-.1
P.SD	8.4	.0	.64	.06	.52	1.4	.51	1.2
REAL RMSE	.32	TRUE SD	.56	SEPARATION	1.77	PERSON RELIABILITY	.76	

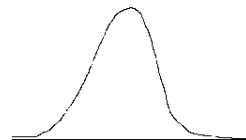
ITEM	13 INPUT	13 MEASURED	INFIT		OUTFIT			
	TOTAL	COUNT	MEASURE	REALSE	IMNSQ	ZSTD	OMNSQ	ZSTD
MEAN	105.2	35.0	.00	.20	1.08	-.3	1.01	-.5
P.SD	25.3	.0	.79	.08	.74	2.6	.70	2.4
REAL RMSE	.21	TRUE SD	.76	SEPARATION	3.55	ITEM RELIABILITY	.93	



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$$\Delta\delta = \tau \cdot \delta; \tau < 0$$



Acquiescence

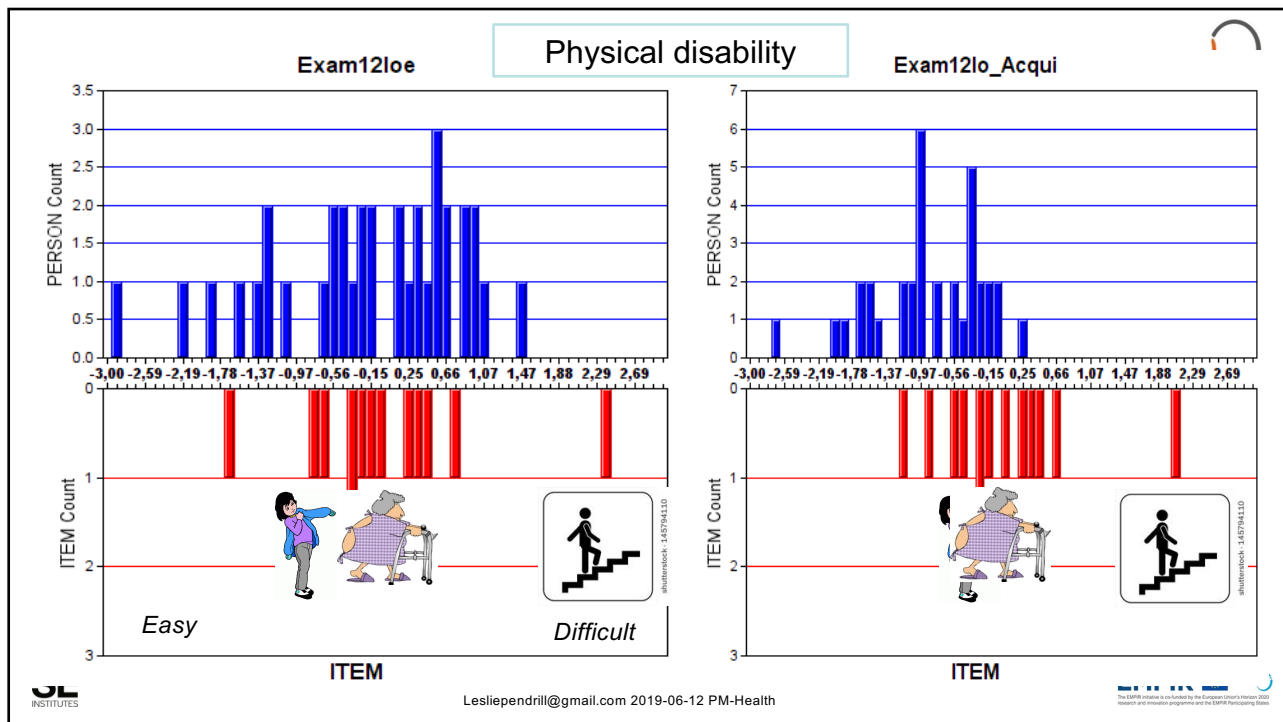
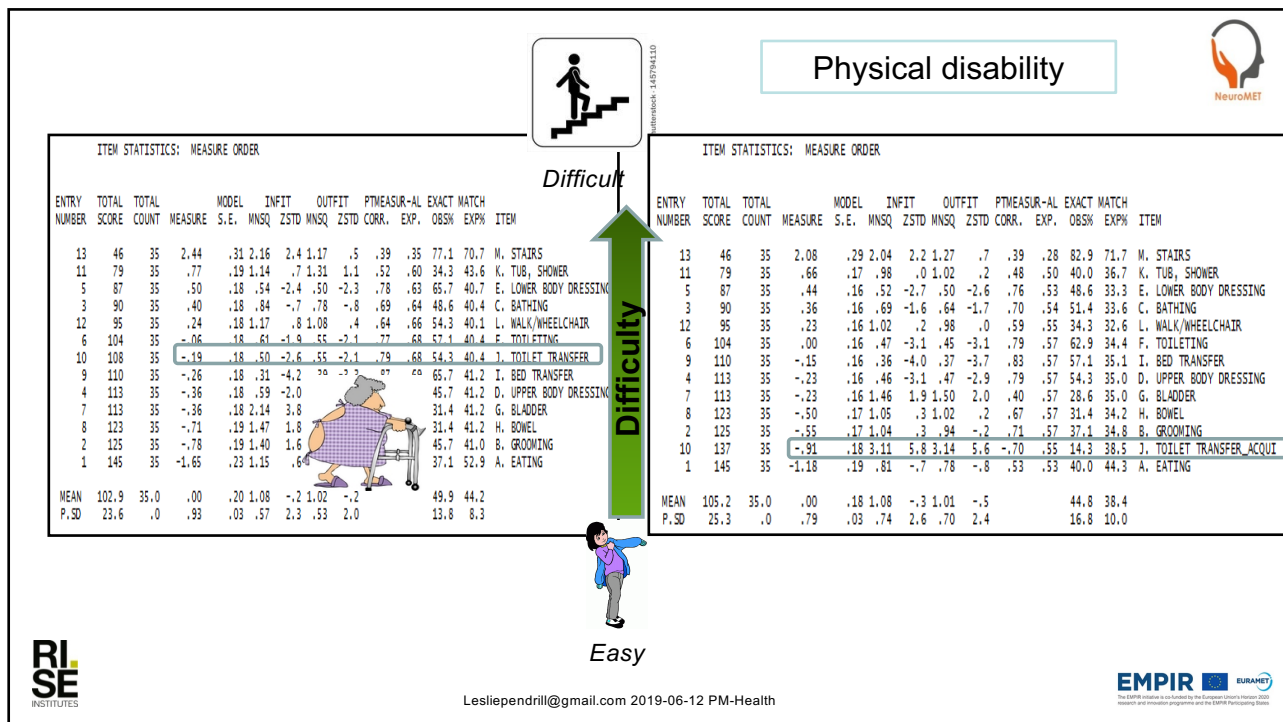
"Agreement regardless of item content"

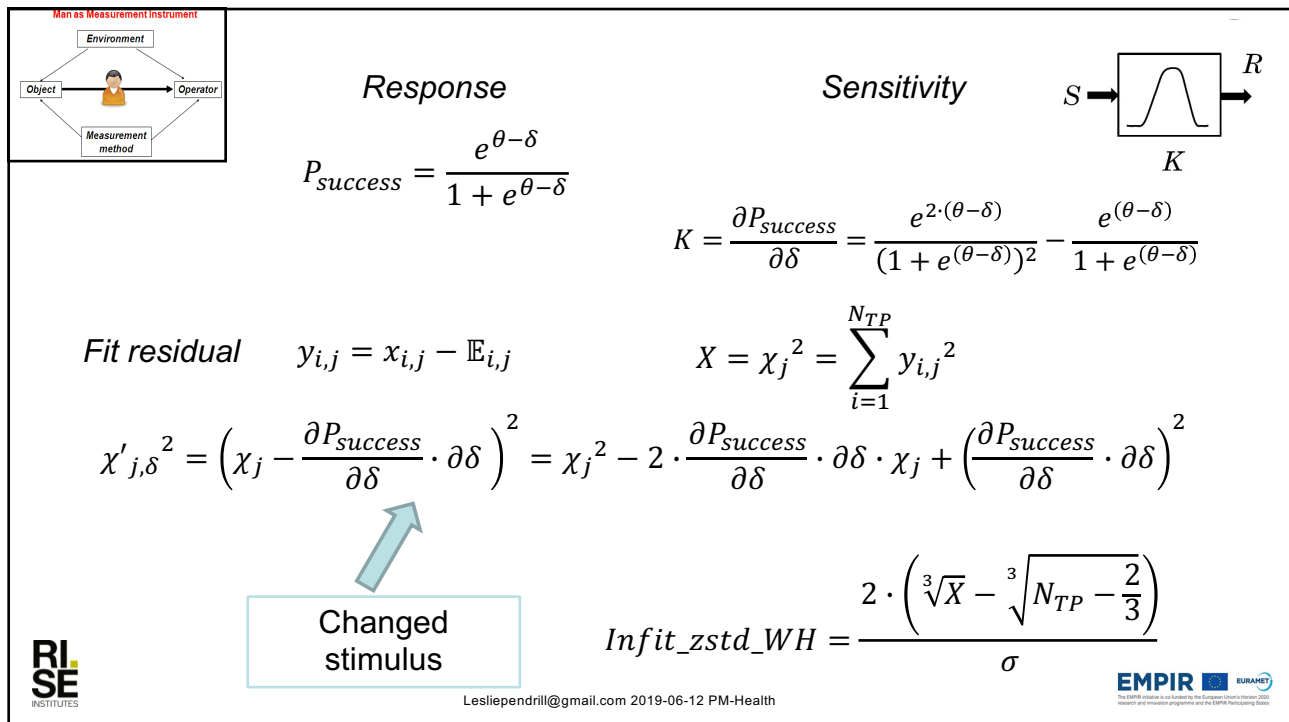
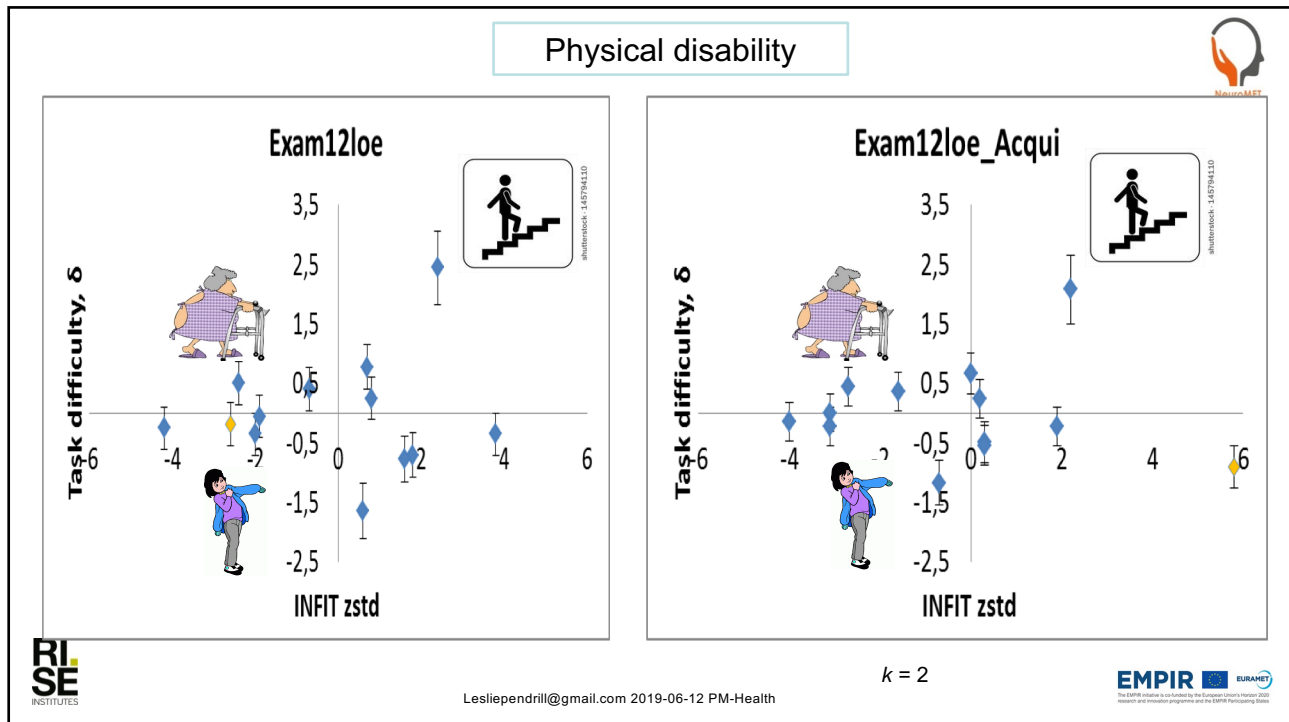
$$P_{success} = \frac{e^{\theta-\delta}}{1 + e^{\theta-\delta}}$$

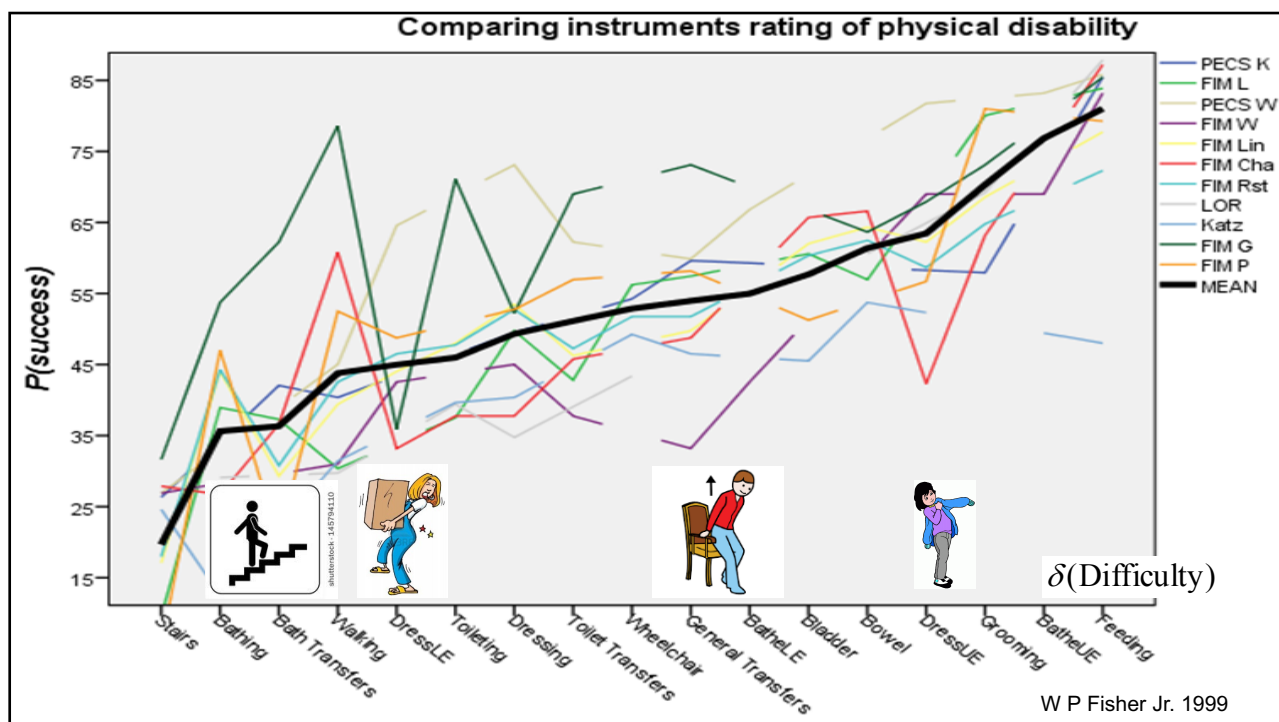
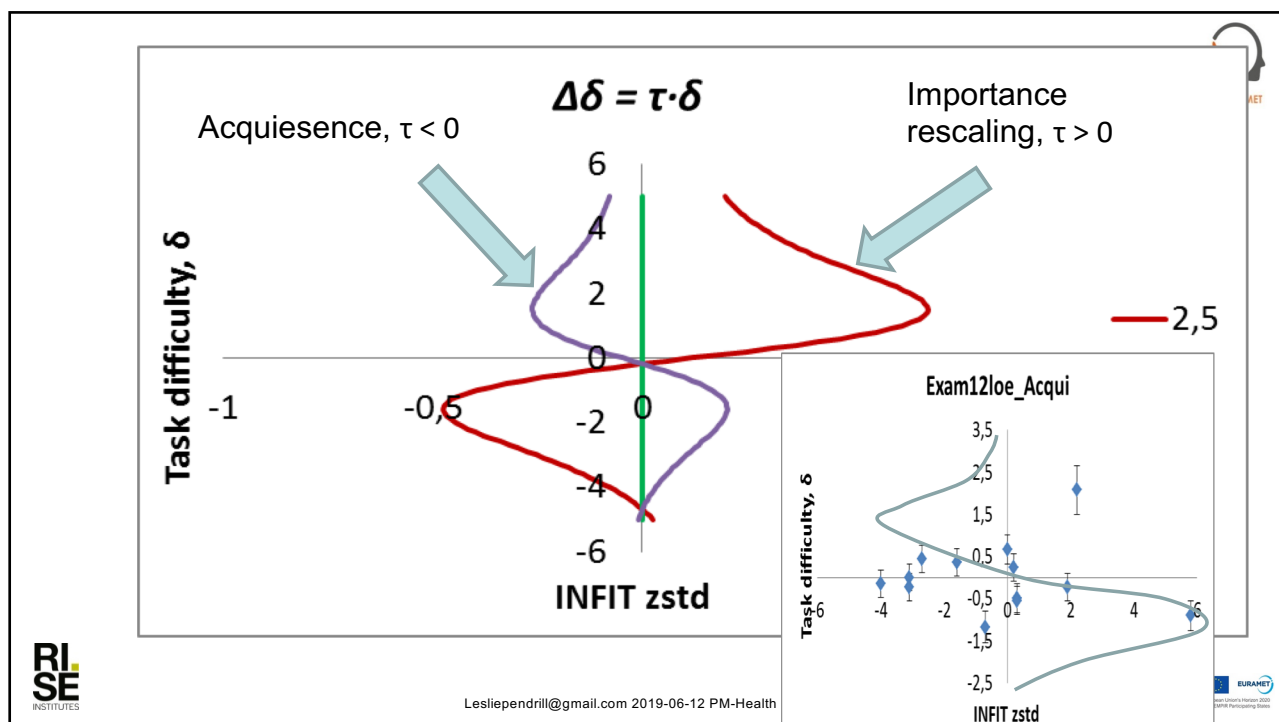


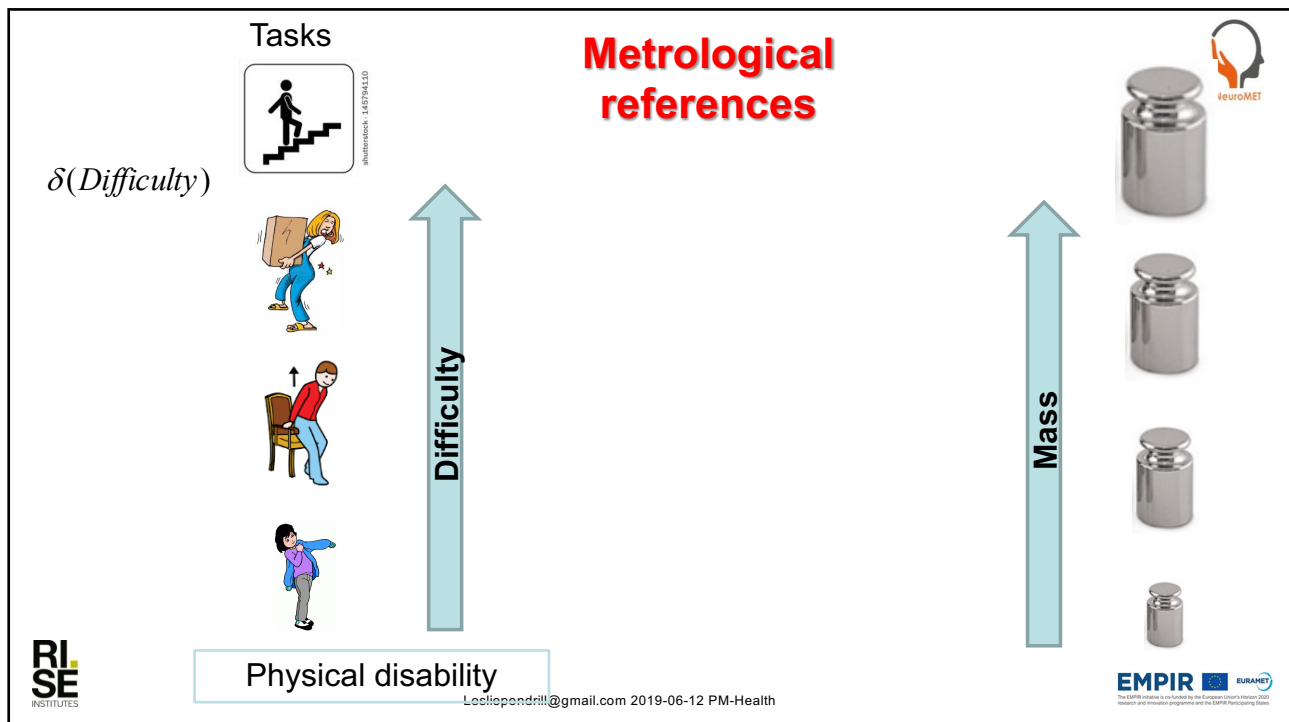
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- Stefan Cano, Modus Outcomes, Boston (USA) & Stotford UK
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Acknowledgments



NeuroMET : www.lgcgroup.com/EMPIR-neuromet



This project has received funding from the EMPIR programme co-financed by the Participating States and from the European Union's Horizon 2020 research and innovation programme

NeuroMET: Innovative measurements for improved diagnosis and management of neurodegenerative diseases

EURAMET's Research Programmes



SI Unit



Environment



Energy



Fundamental



Health



Industry

- EURAMET's research programmes (EMRP and EMPIR) support the collaboration of European metrology institutes, industrial organisations and academia through Joint Research Projects (JRPs). They are structured around European Grand Challenges in such areas as Health, Energy, the Environment and also aim to progress fundamental science.

- See <https://www.euramet.org/> for more details.

EMRP
European Metrology Research Programme
Programme of EURAMET



The EMRP is jointly funded by the EMRP participating countries within EURAMET and the European Union

EMPIR



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